

MATH360. ADVANCED CALCULUS

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Homeworks

1. DUE SEPT 17

1. Simplify the expression:

$$(A \setminus (A \cap B)) \cup (B \setminus (B \setminus A)).$$

(2pts)

2. Show that the following sets are countable:

a) The set \mathbb{Z} of all integers. (3pts)

b) The set $\mathbb{Z}[x]$ of all polynomials in x with integer coefficients. (6pts)

3. How many different sets one can construct from 10 given subsets of a set X using the operations \cap , \cup and $\bar{}$ ($\bar{A} := X \setminus A$)?

(E.g. from one set A one can construct 4 sets: A itself, \bar{A} , $\emptyset = A \cap \bar{A}$ and $X = A \cup \bar{A}$). (5pts)

4. Prove by induction:

a) $1^3 + 2^3 + \cdots + n^3 = (1 + 2 + \cdots + n)^2$. (2pts)

b) The last digit of N^5 is the same as the last digit of N . (2pts)

5. Which relations are transitive:

a) being relative, b) being acquaintance, c) being ancestor? (2pts)

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