

**Fall 2010**

2. Let

$$f(x) = \begin{cases} \frac{x}{x^2+1} & x \leq 1 \\ ax^2 + bx + 1 & x > 1 \end{cases}$$

Find the values of  $a$  and  $b$  so that  $f$  is differentiable everywhere.

- A)  $a = -\frac{1}{2}$  and  $b = 0$     B)  $a = \frac{1}{2}$  and  $b = -1$     C)  $a = -1$  and  $b = \frac{1}{2}$     D)  $a = 1$  and  $b = -\frac{3}{2}$   
E)  $a = 1$  and  $b = 0$     F)  $a = -1$  and  $b = -\frac{1}{2}$     G)  $a = -\frac{3}{2}$  and  $b = 0$     H) No such values

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3. Values of functions  $f, g, f'$ , and  $g'$  are given in the table below:

$x$	-1	0	1	2
$f$	11	7	5	5
$g$	-3	2	-1	1
$f'$	1	3	4	7
$g'$	2	1	5	2

Let  $h(x) = f(g(x)) \cdot g(x)$ . What is  $h'(1)$ ?

- A) -5    B) 0    C) 1    D) 25    E) 40    F) 50    G) 100    H) 250

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6. At how many different values of  $x$  does the curve  $y = x^3 - 2x$  have a tangent line parallel to the line  $y = x$ ?
- |      |      |
|------|------|
| a. 0 | e. 4 |
| b. 1 | f. 5 |
| c. 2 | g. 6 |
| d. 3 | h. 7 |

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7. Find the slope of the tangent line to the curve  $y = \frac{1}{1+2x}$  at the point  $(1, \frac{1}{3})$ .
- |                   |                   |
|-------------------|-------------------|
| a. $-\frac{1}{4}$ | e. $-\frac{2}{9}$ |
| b. 2              | f. -2             |
| c. -1             | g. 1              |
| d. $\frac{1}{4}$  | h. $\frac{1}{2}$  |

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8. If  $f(x) = \sqrt[3]{x^2 - 1}$ , find  $f''(3)$ .

- a.  $\frac{1}{4}$
- b.  $\frac{1}{12}$
- c.  $-\frac{1}{12}$
- d.  $\frac{3}{4}$

- e.  $\frac{1}{3}$
- f.  $\frac{4}{3}$
- g.  $-\frac{4}{3}$
- h. None of these

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8. The curve  $y = x^3 + x^2 - x$  has two horizontal tangents. Find the distance between these two horizontal lines.

a)  $\frac{11}{9}$       b)  $\frac{22}{27}$       c)  $\frac{32}{27}$       d)  $\frac{5}{3}$

e)  $\frac{14}{9}$       f)  $\frac{4}{3}$       g)  $\frac{13}{9}$       h)  $\frac{7}{3}$

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9. If  $f(x) = \frac{x}{\tan x}$ , find  $f'\left(\frac{\pi}{4}\right)$ .

a)  $\frac{2-\pi}{2}$

b)  $\frac{1-\pi}{2}$

c)  $1-\pi$

d)  $\frac{\pi}{2}$

e)  $1-2\pi$

f)  $2-\pi$

g)  $2-2\pi$

h)  $-\pi$

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5. Suppose  $f(3)=2$ ,  $f'(3)=5$ , and  $f''(3)=-2$ . Let  $g(x)=\left[f(x)\right]^2$ . Then  $g''(3)=$

- A) 42      C) 21      E) 5      G) -20  
B) 20      D) 10      F) 38      H) None of these

**Hand In HW #4**  
**Answer Section**

**Fall 2010 # 2: B**

**Fall 2010 # 3: F**

**Spring 2010 # 6: C**

**Spring 2010 # 7: E**

**Spring 2010 # 8: C**

**Fall 2009 # 8: C**

**Fall 2009 # 9: A**

**Spring 2009 # 5: A**