

1. Use the rules to find the derivative of each function. No need to "simplify".

$$(i) \quad y = f(x) = \frac{1}{(x^4 - 4x^3 + 8)^3}$$

$$(ii) \quad y = f(x) = \tan^{-1}(e^{x^2})$$

$$(iii) \quad y = f(x) = \ln(\ln(\ln(4x^2)))$$

$$(iv) \quad y = f(x) = \ln(\sqrt{x})\sqrt{\ln x}$$

$$(v) \quad y = f(x) = \sin^{-1}(2x) \sin 2x$$

$$(vi) \quad y = f(x) = e^{e^{9x}}$$

$$(vii) \quad y = f(x) = (x^3 + 3x + 1)^5 (x^4 - 3x^3 + 1)^4$$

2. Let  $y = f(x) = 2x^5 + x^3 + 1$ . Let  $g(x) = f^{-1}(x)$ , the **inverse** function of  $f(x)$ . Find  $g'(4)$  [ $= f^{-1}'(4)$ ]

3. Find the equation of the line tangent to the graph of  $x \ln y + e^{xy} - y = 0$  at the graph point  $(0,1)$  .

4. Use linearization (the tangent line) to estimate the number  $\sqrt[3]{1001}$ .  
(Decimal answer is neither required nor desired)

5. Find  $\frac{dy}{dx} = f'(x)$  if  $y = f(x) = \frac{(x^2 - 8)^{\frac{1}{3}} \sqrt{x^3 + 1}}{(x^6 - 7x + 1)e^x}$

6.

Values of functions  $f, g, f'$ , and  $g'$  are given in the table below:

$x$	-1	0	1	2
$f$	11	7	5	5
$g$	-3	2	-1	1
$f'$	1	3	4	7
$g'$	2	1	5	2

If  $h(x) = f(g(x))$ , what is  $h'(1)$ ?

7. A conical water tank with vertex down has a radius of 10 ft at the top and is 24 ft high. Water flows into the tank at a rate of  $20 \text{ ft}^3$  per minute. How fast is the depth of the water increasing when the water is 16 ft deep?

Note: The volume of a (right, circular) cone is  $V = \frac{1}{3}\pi r^2 h$